

Optimal commitment under uncertainty: adjustment rules for climate policy

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Abstract

This paper analyses the optimal type and degree of commitment to a future climate policy when damage costs from climate change are uncertain. Taking uncertainty into account, it is shown within the framework of a sequential game between firms and a regulator that commitment to an emission abatement target fails to achieve the first best optimal outcome. Though commitment to a future policy reduces the risk of time-inconsistency, it imposes costs in the form of reduced flexibility to respond to new information. If, however, the regulator commits to an adjustment rule that sets the abatement level contingent on the realization of the uncertain parameter, the first best optimal outcome can be obtained.

Keywords: time-inconsistency, commitment, adjustment rule

JEL classifications: D81, H23, H32, O31

1 Introduction

Emissions of greenhouse gases contribute to climate change. Regulators, by putting a price on such emissions, can encourage firms to invest in the development and deployment of technologies that reduce emissions and thereby climate change. Firms may, however, doubt the stability of that policy over time if the regulator is perceived to have an *ex-post* incentive to renege on a policy that was optimal *ex-ante*; a phenomenon known as ‘time-inconsistency’ (Kydland and Prescott 1977, Helm et al. 2003). A lack of confidence in the future stability of a policy reduces the effectiveness of that policy today. The perceived risk of policy change increases the cost of achieving any given level of emissions abatement.

The question of how to make climate policy more stable and credible figures prominently in discussions surrounding the reform of the EU emission trading scheme (EU ETS) (Grosjean et al., submitted). Following the sharp drop of prices for emission permits from about 30 Euros in January 2008 to less than 5 Euros in December 2013 several adjustments have been proposed such as reducing the number of emission permits and other interventions (European Commission 2012). All proposals imply a trade-off, often unmentioned and unresolved, that is fundamental for the design of long-term policies: while on the one hand policy makers aim to establish credible carbon price signals to investors and innovators, they also seek flexibility in order to be able to react to unforeseen developments in the market, politics, and science (Brunner et al. 2012).

One important source of uncertainty that policy makers seek to address in climate policy concerns the cost of climate change which is a composite of many uncertain parameters including climate sensitivity, regional impacts, and economic growth. Consider for instance climate sensitivity: a doubling of the concentration of greenhouse gases in the atmosphere would likely increase the global mean surface temperature between 1.5°C

30 and 4°C according to the Intergovernmental Panel on Climate Change (IPCC 2013). This
31 range is fairly broad and newer evidence suggests that it is too low (Shiogama and
32 Ogura 2014). Uncertainty over climate sensitivity is amplified by uncertainties on how a
33 changing climate translates into actual impacts (such as draughts, sea-level rise or
34 tropical storms) and lack of knowledge how societies can adapt to them (Malik and
35 Smith 2012). For this reason, new knowledge on any of the above and other parameters
36 could in the future make it desirable to opt for either more or less stringent emission
37 reduction targets than what seems optimal from the current perspective. How can the
38 trade-off between flexibility and commitment in climate policy be mitigated? The
39 central insight conveyed by our analysis is that policy makers can reconcile this trade-off
40 by committing to a transparent rule that allows readjusting the abatement target
41 conditional on new information.

42

43 The remainder of this paper proceeds as follows: Section 2 sketches the theoretical
44 background behind time-inconsistency in climate policy. Section 3 presents a
45 deterministic Stackelberg game to demonstrate how (i) time-inconsistency emerges if
46 firms move first, and (ii) the social optimum can be obtained if the regulator can commit
47 to a certain policy level. We then introduce a term into the regulator's objective
48 function that punishes deviations from announced policies to generalize the polar cases
49 of full commitment and no commitment and include settings with intermediate
50 commitment. Section 4 derives the optimal level of commitment under uncertainty and
51 shows that the first best outcome can only be achieved if the regulator commits to an
52 adjustment rule that sets the abatement level contingent on the realization of climate
53 change damage costs. Section 5 discusses policy design options of commitment devices
54 and adjustment rules. Section 6 concludes.

55

56

57 **2 Motivation and theoretical background**

58

59 It is well recognized in the literature that in a dynamic setting, multiple objectives of
60 which not all are directly addressed by specific policy instruments can give rise to time-
61 inconsistency (Helm et al. 2003). For example, when designing and implementing
62 climate policies, policy makers also tend to take into account industry competitiveness,
63 effects on tax revenues, and distributional issues. Changes in these dimensions can
64 make it desirable to deviate from previously announced emission reduction targets. For
65 instance, Canada's withdrawal from the Kyoto protocol in 2011, and Japan's recent
66 refusal to participate in its extension beyond the commitment period that ended in 2012
67 point to important incentives to deviate from previously announced targets though
68 there is no consensus on the exact reasoning behind these government decisions. The
69 same can be stated for the case of Australia, for which the new government appointed
70 in mid-2013 announced a repeal of the carbon-tax introduced by its predecessor in 2012
71 (Guardian 2013).

72

73 In the context of climate policy, it has frequently been observed that the development
74 and adoption of innovative low-carbon technologies by the private sector may be
75 impeded by time-inconsistency: in order to provide incentives for firms to undertake
76 irreversible investments in R&D, the regulator has to guarantee a relatively high future
77 carbon price (Miliman and Prince 1989, Nordhaus 2011). Once these investments are
78 undertaken, however, the socially optimal *ex post* carbon price set by the regulator is
79 too low for firms to recoup their investment (Kennedy and Laplante 2000; Requate and
80 Unold 2003; Montgomery and Smith 2005). As firms anticipate this policy change, the
81 regulator's guarantee is not credible and under-investment results.

82

83 Previous literature has pointed out that a regulator's best response to the problem of
84 time-inconsistency is to credibly commit to the *ex-ante* optimal policy level (e.g.
85 Biglaiser et al. 1995; Gersbach and Glazer 1999; Helm et al. 2004). This literature tends

86 to assume a deterministic settings in which there is no uncertainty over modelled
87 parameters. In these settings, the regulator typically pursues two policy targets – the
88 firm’s technology choice and abatement effort – with a single policy instrument. With
89 credible commitment to the ex-ante optimal policy level, firms’ incentives to influence
90 the regulator’s *ex-post* choice are removed and the first best outcome is achieved
91 (Kennedy and Laplante 2000; Ulph and Ulph 2013). Obtaining the first-best outcome
92 rests on the assumption that no market failures or behavioral barriers other than the
93 emissions externality exist (Staub-Kaminski et al., forthcoming) or, if they do exist, they
94 get addressed by optimal policy instruments (e.g. R&D subsidies to internalize
95 technology spill-overs, see Jaffe et al. 2005).

96

97 Previous literature has also looked at how the type of policy instrument can matter for
98 optimality in settings of time-inconsistency. As has been pointed out by Ulph and Ulph
99 (2013), the first-best optimal outcome can be obtained with committing to a quantity
100 target but not with commitment to a certain tax level. With a carbon tax, the regulator
101 would instead need to commit to implement the tax that achieves the ex ante optimal
102 emission level (without responding to firms’ actions), which translates in a menu of tax
103 levels contingent on firms’ investment behavior. For the purpose of this paper, we
104 analyze the case in which the regulator commits to a certain level of emission
105 abatement. This could be achieved either via a quantity instrument, or a menu of
106 conditional carbon taxes as in Ulph and Ulph (2013). We show that if one acknowledges
107 the presence of uncertainty regarding the costs of climate change damages, full
108 commitment to an abatement target – identified as optimal in a deterministic setting –
109 leads to suboptimal outcomes. As uncertainty is pervasive in climate change policy
110 decisions (Kunreuther et al. 2013), devising a mechanism that combines credible
111 incentives with policy flexibility may prove useful.

112

113 By expanding the stylized dichotomy between ‘full commitment’ and ‘no commitment’
114 frequently adopted in the literature, we show that in a setting in which the regulator

115 commits to a policy level, an intermediate degree of commitment is optimal under
116 uncertainty (as it is then desirable to retain some policy flexibility in order to respond to
117 new information). We then demonstrate that if the resolution of uncertainty can be
118 observed *ex-post* and the regulator can commit to a state-contingent rule that
119 determines the amount of emission abatement as a function of climate change damage
120 costs the first best outcome can be obtained.

121

122 In this paper we employ a Stackelberg framework, in which the regulator first
123 announces its emission target and then firms decide on investment and abatement once
124 uncertainty is resolved. This modeling framework captures some essential features of
125 real-world issues. First, in order to send credible signals to the private sector, policy
126 makers announce long-term abatement targets which are only altered on rare
127 occasions. Second, uncertainty is – at least partially – resolved by new information that
128 becomes available only after the policy target has been set. Third, firms decide on their
129 investments based on expectations on the future policy enacted by the regulator. We
130 use benefits of climate change mitigation – which to date is one of the most important
131 unknowns regarding the formulation of climate policies – as an illustration of an
132 uncertain parameter.

133

134

135 **3 Full, no, and intermediate commitment in a deterministic** 136 **setting**

137

138 One example for time-inconsistency is when a regulator announces a future climate
139 policy *ex ante* but faces an incentive to change the policy after the regulated entities
140 have taken their investment decisions. Consider a regulator who decides about the
141 aggregate level of emissions abatement e (the climate policy) to be provided by firms
142 that can lower their abatement costs by investing in technology t at R&D costs $\mathcal{G}(t)$,

143 with $\mathcal{G}_t(t) > 0$.¹ Let $b(e)$ and $c(e, t)$ denote the (social) benefits and (firms') costs of e ,
 144 respectively, with $b_e(e) > 0$, $c_e(e, t) > 0$, and $c_t(e, t) < 0$. For an interior solution, we also
 145 assume $b_{ee}(e) \leq 0$, $c_{ee}(e, t) \geq 0$, $c_{et}(e, t) \leq 0$. Throughout this paper, we assume that all
 146 parameters determining the firms' as well as the regulator's decisions are public
 147 knowledge².

148

149 The first-best optimal solution is obtained maximizing the following social welfare
 150 function:

151

$$152 \quad W = b(e) - c(e, t) - \mathcal{G}(t) \tag{1}$$

153

154 Calculating the derivatives yields the following first-order conditions for the optimal
 155 values of e and t :

156

$$157 \quad \text{(i) } b_e(e^{opt}) = c_e(e^{opt}, t^{opt}), \text{ and} \tag{2}$$

$$158 \quad \text{(ii) } c_t(e^{opt}, t^{opt}) + \mathcal{G}_t(t^{opt}) = 0. \tag{3}$$

159

160 Let us consider a three stage game à la Stackelberg. First, the regulator announces its
 161 abatement target e . Second, firms invest in emission saving technologies. In the final
 162 stage of the game, the regulator implements a policy to achieve the socially optimal
 163 level of abatement e . This formulation captures essential properties of long-term
 164 climate policy.

165

166 Lemma 1: *If the regulator can commit to e , the socially optimal outcome can be*
 167 *obtained.*

168

¹ Subscripts denote partial derivatives.

² There exists a gap in the literature because the problem of time-inconsistency under asymmetric information has – with the notable exception of Boyer and Laffont (1999) – hitherto not been analyzed.

169 Proof: In the decentralized solution, firms choose their level of technology t to minimize
 170 their total costs $c(e,t) + \theta(t)$. If the regulator is able to commit to its choice of e , it opts
 171 for e^{opt} in the final stage, firms choose technology t^{opt} , and the optimal outcome is
 172 obtained. \square

173

174 Lemma 2: *If the regulator is unable to commit to the announced level of e , the firms*
 175 *choose technology level t which is below the social optimum as compared to the case*
 176 *with credible commitment. The same holds for the regulator's choice of e .*

177

178 Proof: If the commitment is not credible, firms anticipate the regulator's reaction when
 179 deciding their level of technology. In this case, the regulator's first-order condition in the
 180 final and decisive period, taking the firms choice of technology t^f as given, becomes:

181

$$182 \quad b_e(e^{reg}) = c_e(e^{reg}, t^f). \quad (4)$$

183

184 This condition implicitly defines the regulator's reaction function to firms' choice of

185 technology. It can easily be verified that $\frac{de^{reg}}{dt^f} > 0$, i.e. the regulator responds to firms'

186 choice of a lower level of technology by adopting a less ambitious emissions abatement

187 target. The firms' technology choice is determined by their cost minimization problem,

188 taking into account the regulator's reaction function:

189

$$190 \quad \min_t [c(e,t) + \theta(t)] \Rightarrow$$

$$191 \quad c_e(e^{reg}, t^f) \frac{de^{reg}}{dt^f} + c_t(e^{reg}, t^f) + \theta_t(t^f) = 0. \quad (5)$$

192

193 As the first term is positive, $c_t(e^{reg}, t^f) + \theta_t(t^f) < 0$. This means that the social cost of

194 supplying e is not at a minimum, as would be required by the optimality condition

195 $c_t(e,t) + \theta_t(t) = 0$, but could be further decreased by increasing t . However, given the

196 regulator's reaction function, such an increase in t would also raise the total level of
197 emissions abatement e that firms are required to provide. \square

198

199 As firms anticipate that lower marginal costs due to technological innovation will
200 prompt the regulator to adopt more stringent policy, they choose a level of technology
201 below the social optimum. In our model, this 'ratchet effect' (Weitzman, 1980), which is
202 due to the regulator's flexibility to react to firms' choice of t , results in a time-
203 inconsistent choice of the abatement target e .³ However, this problem can be overcome
204 if the regulator has a means to credibly commit to its future actions. A commitment is
205 only credible if the cost of breaking it exceeds the potential gains from deviation
206 (Schelling, 1960). The regulator hence only has an incentive to adhere to a prior
207 commitment if deviation results in a punishment that is sufficiently large. Such
208 punishments, which are discussed in more detail in Section 5, can e.g. include bad press
209 and loss of reputation, a lower likelihood of being re-elected, or actual financial costs. If
210 the punishment depends on the magnitude of the deviation from the announced policy,
211 the regulator's optimal *ex-post* policy is determined by its *ex-ante* commitment and the
212 severity of the punishment. For the case in which the punishment for an infinitesimally
213 small deviation from the announced policy approaches infinity, the regulator never has
214 an incentive to deviate from the announced policy and full commitment is obtained.

215

216 *Lemma 3: The cases of 'full commitment' and 'no commitment' as well as all*
217 *intermediate cases can be modeled by introducing a punishment function Θ into the*
218 *regulator's objective function. Punishment of deviations from an announced policy then*
219 *acts as a commitment device.*

220

221 **Proof:** Let the regulator's objective function be

³ Note that by modeling one representative firm, we implicitly assume that firms are able to coordinate their actions. If a single firm's action has no influence on the regulator's reaction, the problem of time-inconsistency does not arise in our framework. Thus the formulation chosen here can be expected to be suitable for monopolistic markets such as power generation in many countries.

222

223 $W = b(e) - c(e, t) - \mathcal{G}(t) - \Theta(|e - e^{opt}|)$ with $\Theta' > 0$. (6)

224

225 Obviously, the case of no commitment is obtained for $\Theta(e) = 0$. Furthermore, it can be

226 easily verified that $\frac{de^{reg}}{dt^f} \rightarrow 0$ for $\Theta(e \neq e^{opt}) \rightarrow \infty$, yielding the full commitment setup.

227 Between these polar cases lies a continuum of setups in which the regulator is punished

228 for deviations from the pre-announced policy. \square

229

230 With perfect foresight, it is clear that perfect regulatory commitment is the most
231 desirable option from a social perspective (under the assumptions of our model).

232 However, in presence of uncertainties with regard to benefits and costs of emissions

233 abatement, some flexibility to deviate from prior announcements in order to react to

234 unforeseen events can prove advantageous. Therefore, as we show in the next section,

235 there is a trade-off between providing stable incentives for investments in emissions

236 abatement on the one hand and retaining the flexibility to accommodate new

237 information on the other.

238

239 **4 Commitment under uncertainty**

240

241 We outline a simple analytical model with linear benefits, quadratic abatement costs

242 that decrease linearly in technology t , and a quadratic R&D investment cost function to

243 acquire technology level t , characterized by the parameter k . We analyze the impacts of

244 additive uncertainty in the slope of the benefit function⁴, characterized by its expected

245 value b and the realization of a random shock ε . With mean value 0 and a finite standard

⁴ In climate policy, the largest sources of uncertainty relate to the damage costs of climate change (IPCC 2007). At the same time, uncertainties regarding mitigation costs and costs of technology development undeniably play important roles, too.

246 deviation σ .⁵ We assume that the magnitude of the regulator's punishment Θ for
 247 deviating from an announced target is characterized by the non-negative parameter θ
 248 and quadratic in the difference between the announcement e^* and the actually
 249 implemented level e' . This formulation of a commitment device can be understood in
 250 terms of the reputational costs associated to violating a pledge à la Barro and Gordon
 251 (1983), or political costs in terms of renegotiating legislation (Brunner et al. 2012).
 252 Monetary costs can be introduced in an emission trading system by means of put
 253 options that obligate the regulator to buy back permits at a pre-defined price in the
 254 future (Ismer and Neuhoff 2009). In Section 5, design options of commitment devices
 255 are discussed in more detail.

256

257 The model is hence fully specified by the following set of equations:

258

$$b(e) = (b + \varepsilon)e'; \quad E(\varepsilon) = 0; \quad \text{Var}(\varepsilon) = \sigma^2; \quad \sigma^2 < \infty$$

$$c(e) = \frac{1}{2}ce'^2 - te'$$

259

$$g(t) = \frac{1}{2}kt^2 \tag{7}$$

$$\Theta(e', e^*) = \frac{1}{2}\theta(e' - e^*)^2.$$

260

261 We require all parameters b , c , k and θ as well as the choice variable t to be non-
 262 negative. The social welfare function is given by:

263

$$264 \quad W = (b + \varepsilon)e' - \frac{1}{2}ce'^2 + te' - \frac{1}{2}kt^2 - \frac{1}{2}\theta(e' - e^*)^2 \tag{8}$$

265

266 Again, the game proceeds in three stages: In the first stage, the regulator (R) announces
 267 the target e^* which it aims to implement in the final stage. In the second stage, the

⁵ See Weitzman (2009) on limitations of expected utility theory for distributions with an infinite standard deviation.

268 uncertainty regarding benefits is resolved and firms (F) choose their level of technology
 269 t .⁶ In the third stage, the regulator decides on the level of emissions abatement that is
 270 actually implemented (e'), given the realization of the new information ε regarding
 271 benefits as well as firms' choice of t , and firms supply e' at the corresponding cost
 272 function ([Figure 1](#)).

273

274

[Figure 1 about here]

275

276 The decentralized nature of the strategic interaction between the regulator and the
 277 regulated firms requires both players to form expectations of future scenarios (which
 278 are determined by the other player's action, and, for the regulator, the possible
 279 realization of the shock). To solve the problem, we apply backward induction from the
 280 third to the second and finally to the first stage.

281

282 *The Third Stage*

283 In the third stage, the regulator chooses e' , the level of emissions abatement to be
 284 performed by the firms, taking as given technology t , the realization of the shock ε , as
 285 well as e^* (its own announcement of the first stage). Its maximization problem then
 286 yields:

287

$$288 \quad e' = \arg \max_{e'} [W] = \arg \max_{e'} \left[(b + \varepsilon)e' - \frac{1}{2}ce'^2 + te' - \frac{1}{2}kt^2 - \frac{1}{2}\theta(e' - e^*)^2 \right] \Rightarrow$$

$$e' = \frac{(b + \varepsilon) + t + \theta e^*}{c + \theta}.$$

289

290 The level of emissions abatement that the regulator requires firms to supply is the
 291 higher (i) the larger actual benefits, i.e. $(b + \varepsilon)$, (ii) the higher the firms' level of

⁶ Hence, firms do not face uncertainty when deciding on their technology level.

292 technology t , (iii) the more ambitious the announced target e^* , and (iv) the lower
293 abatement costs, characterized by c .

294

295 *The Second Stage*

296 In the second stage, firms take the regulator's announced policy e^* as given from the
297 first stage and anticipate how the former will react in the third stage to their second
298 stage choice of t and the shock ε . Firms observe the shock ε occurring to the benefit
299 function and decide which level of technology to employ in order minimize their total
300 costs:

301

$$302 \quad t' = \arg \min_t \frac{1}{2} c e'(\varepsilon, t, e^*)^2 - t e'(\varepsilon, t, e^*) + \frac{1}{2} k t^2. \quad (10)$$

303 As firms are able to solve the regulator's decision problem in the third stage, inserting e'
304 in Eq.(10) results in the following solution for the firms' technology choice t' :

305

$$306 \quad t' = \frac{\theta(b + \varepsilon) + \theta^2 e^*}{k(c + \theta)^2 - c - 2\theta}. \quad (11)$$

307

308 In order to ensure that $t' > 0$, let us assume that the condition $k > \frac{c + 2\theta}{(c + \theta)^2}$ holds.⁷ Then,

309 t' increases with (i) actual benefits $(b + \varepsilon)$, (ii) the regulator's announced policy e^* , and
310 (iii) the strength of the regulator's commitment to its announced target (θ) , as all
311 parameters cause firms to anticipate that stricter requirements will be put into place by
312 the regulator in stage three.

313

314

⁷ Otherwise, firms would have an incentive to choose a negative level of technology that raises their costs, in order to prompt the regulator to choose a laxer abatement target.

315 *The First Stage*

316 In order to be able to decide which target e^* to announce before knowing the actual
317 realization of ε , the regulator has to form expectations about social welfare under all
318 possible outcomes. Plugging the expressions for e^* and t^* into the welfare function and
319 rearranging terms results in:

$$321 \quad W = \frac{[\theta e^* + b + \varepsilon]^2 [(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2] - \theta [k(c + \theta)^2 - c - 2\theta]^2 e^{*2}}{2[k(c + \theta)^2 - c - 2\theta]^2}. \quad (12)$$

322

323 Taking expectations then yields:

324

$$325 \quad W^e = \frac{[\theta^2 e^{*2} + b^2 + 2b\theta e^* + \sigma^2] [(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2] - \theta [k(c + \theta)^2 - c - 2\theta]^2 e^{*2}}{2[k(c + \theta)^2 - c - 2\theta]^2}. \quad (13)$$

326

327 Maximizing this expression with respect to e^* gives us the regulator's optimal choice of
328 e^* , as a function of the underlying parameters:

329

$$330 \quad e^* = \frac{b[(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2]}{[k(c + \theta)^2 - c - 2\theta]^2 - \theta [(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2]}. \quad (14)$$

331

332

333 *Welfare*

334 Inserting e^* into the expression for expected welfare and rearranging terms yields:

335

$$336 \quad W^e = \frac{b^2 [(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2]}{2[k(c + \theta)^2 - c - 2\theta]^2 - 2\theta [(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2]} \quad (15)$$
$$+ \frac{\sigma^2 [(k(c + \theta) - 1)^2 (c + \theta) - k\theta^2]}{2[k(c + \theta)^2 - c - 2\theta]^2}.$$

337

338

339 Proposition 1: With uncertainty and commitment to a pre-announced policy e^* , neither
 340 the case of full nor the case of no commitment yields the optimal result. Rather, in this
 341 setting an intermediate value of θ (i.e. $0 < \theta < \infty$) provides the socially optimal mix of
 342 commitment and flexibility.

343

344 Proof: Calculating the derivative of expected welfare with respect to θ and evaluating

345 the expression at the extreme values $\theta = 0$ and $\theta \rightarrow \infty$ shows that $\left. \frac{\partial W^e}{\partial \theta} \right|_{\theta=0} > 0$ and

346 $\left. \frac{\partial W^e}{\partial \theta} \right|_{\theta \rightarrow \infty} < 0$. \square

347

348 From a social welfare point of view, it is desirable to choose the value of θ such that it
 349 maximizes expected welfare. As maximizing the above expression for expected welfare
 350 would require solving polynomials in fourth order of θ , for which no analytical formulas
 351 exist, it is in general not possible to state the maximum in analytical terms. However, it
 352 is convenient to employ numerical methods⁸ to calculate the values of θ that maximize
 353 W^e for different sets of parameters. The result of this exercise is shown in [Figure 2](#),
 354 which plots the optimal value of θ as a function of b^2 / σ^2 . This set of graphs⁹ suggests
 355 that the optimal level of commitment (i) increases as expected benefits b increase and
 356 uncertainty σ decreases, and (ii) decreases with higher abatement costs – characterized
 357 by c – as well as technology costs k . This finding is in line with intuition: the optimal level
 358 of commitment is the higher the higher the benefits of mitigation relative to costs, and
 359 the lower uncertainty over benefits. One can expect that this relationship holds for a
 360 broad class of models, independent of the specific functional form adopted for costs and
 361 benefits.

362

363

⁸ We used Matlab's bounded minimization routine `fminbnd`.

⁹ Note that the optimal ϑ is always strictly positive.

[Figure 2 about here]

364

365

366 *First best solution*

367 As shown by the example in Section 2, the first best outcome can be obtained by

368 simultaneously choosing e and t after observing the realization of ε , such that the first-

369 order conditions $b_e(e^{opt}) = c_e(e^{opt}, t^{opt})$ and $c_t(e^{opt}, t^{opt}) + \mathcal{G}_t(t^{opt}) = 0$ are fulfilled. This

370 would result in the following policy:

371

$$\begin{aligned} t^{opt} &= \frac{b + \varepsilon}{kc - 1} \\ e^{opt} &= \frac{k(b + \varepsilon)}{kc - 1} \end{aligned} \tag{16}$$

373

374 Plugging these expressions in the social welfare function and taking expectations yields:

375

$$W^{e,fb} = \frac{(b^2 + \sigma^2)}{2(kc - 1)} \tag{17}$$

377

378 *Proposition 2:* With uncertainty, the expected welfare of committing to a pre-announced

379 policy e^* is strictly inferior to the first best optimum, regardless of the level of

380 commitment θ .

381

382 Proof: Comparing expressions for welfare in the commitment under uncertainty case

383 (Eq.(15)) and the first best case (Eq.(17)) reveals that the two expressions differ, i.e. .

384 $W^e \neq W^{e,fb}$. As the first best optimum of Eq.(17) corresponds to the optimal choice of e'

385 and t (which maximizes expected welfare), Eq.(15) has to lie strictly below the level of

386 expected welfare implied by Eq.(17). Hence, Eq.(15) constitutes a second best but not a

387 first best optimum, i.e. it is only optimal under the precondition that the regulator's

388 choice is restricted to committing to a specific abatement level. \square

389

390 *Commitment to an adjustment rule*

391 Under uncertainty, there is no a-priori commitment to a specific e^* that yields the first-
392 best optimal outcome. However, instead of making a commitment to a pre-announced
393 policy the regulator could commit to an adjustment rule that sets e^* contingent on the
394 realization of ε .

395

396 *Proposition 3: The first-best optimal outcome can be achieved if the regulator commits*
397 *to an adjustment rule which implements a certain level of e contingent on the realization*
398 *of the shock ε .*

399

400 Proof: As we have shown in Eq.(16), the first best outcome implies $e^{opt} = \frac{k(b + \varepsilon)}{kc - 1}$ and

401 $t^{opt} = \frac{b + \varepsilon}{kc - 1}$. By announcing the policy $e^* = \frac{kb}{kc - 1}$ and committing to an adjustment rule

402 that includes a punishment term of the form $\Theta(e' - e^*) = \frac{\theta}{2}(e' - e^* - \frac{k\varepsilon}{kc - 1})^2$; $\theta \rightarrow \infty$, the

403 regulator will always adjust its a priori choice of e^* such that the first best level of e'
404 identified in Eq.(16) will be chosen. This commitment strategy deprives firms of their
405 incentive to implement a lower level of technology in order to influence the regulator's
406 choice of e' . As can easily be verified from firms' cost minimization problem, their cost-
407 minimization problem then results in choosing the first best level of technology t^{opt} . \square

408

409 Hence, commitment to a rule that adjusts the policy dependent on the realization of the
410 uncertain variable can be both time-consistent and ex post optimal. At first glance, this
411 finding may appear to be in line with Ulph and Ulph (2013) who show that regulators
412 should commit to a menu of taxes contingent on the firm's investment instead of
413 committing to a certain tax level. However, their reason for proposing an adjustable tax
414 is to discourage strategic behavior by firms. By contrast, our adjustment rule aims at
415 addressing the natural system uncertainty by adjusting the optimal abatement level. Its
416 purpose lies in providing the regulator with flexibility if the best estimate of climate

417 change damage costs varies due to new scientific insights. It thereby goes beyond the
418 deterrence of strategic under-investment by firms toward improving policy resilience
419 under natural system uncertainty. Ulph and Ulph (2013) also show that technology
420 subsidies that remove firms' incentives to under-invest with the aim to influence the
421 regulator to implement a less stringent abatement target can act as a substitute for a
422 commitment device, i.e. it can achieve the socially optimal outcome. This line of
423 reasoning also applies to our setting. In fact, if the subsidy is implemented after the
424 stochastic shock is resolved, our model is equivalent to Ulph and Ulph (2013).

425

426 Practical implementation of an adjustment rule crucially rests on the assumption that
427 the shock is publicly observable. While new information on the physical impacts can
428 clearly be regarded as common knowledge, their economic valuation would require an
429 agreed method to monetize damage costs. For this reason, putting an adjustment rule
430 into practice is expected to be more challenging than stylized model above suggests.

431

432

433 Note that the uncertainty surrounding marginal abatement costs or R&D costs of new
434 technologies – a case not investigated here – also derives from significant information
435 asymmetries between firms and government. The existence of such 'strategic'
436 uncertainty diminishes the value of adjustment rules in the context of time-
437 inconsistency because the contingent variable can be influenced by firm behavior.

438

439 **5 Implementing adjustment rules**

440

441 The punishment term introduced above incurs costs on the government if it decides to
442 deviate from the emission target that results from the adjustment rule. Costs can accrue
443 in various forms: time, bad press, the need to seek cross-partisan consensus, losing
444 votes, admonition from courts, financial expenditures etc.. Devices that incur such costs
445 do not put an absolute limit on government flexibility. Rather, they provide

446 governments with an incentive to adhere to the announced policy rule by decreasing
447 the gains from deviation. Brunner et al. (2012) identify three broader types of
448 commitment devices two of which seem appropriate to implement an adjustment rule
449 for climate policy: legislation and delegation.

450

451 First, legislation provides the legal foundation for the abatement target, the adjustment
452 rule and a transparent governance structure for implementing and updating the policy.
453 Commitment by means of constitutional law presents a high hurdle to policy change
454 because constitutional amendments often require qualified majorities. Instead of
455 changing legal provisions, the incumbent could also decide to ignore laws and
456 regulations. Plausibly, the main motivation for government to avoid non-compliance
457 with the law is public scrutiny. If a governing majority anticipates that the political costs
458 of pursuing a certain course of action will be a loss of public support, then taking this
459 route is less attractive. Hence, climate laws could be designed such as to encourage
460 public scrutiny. This could e.g. be achieved by earmarking revenues from emissions
461 trading to be invested in public infrastructure or recycled back to consumers via annual
462 lump-sum payouts (note that the economic efficiency of earmarking revenues is
463 contested).

464

465 Second, delegating authority to an organization with a time horizon beyond the current
466 legislative period may help to insulate interests dedicated to emissions abatement from
467 day-to-day politics. The climate law may hence establish an independent institution that
468 monitors and advises the government on climate policy. The merit of establishing an
469 independent watchdog lies in forcing government to publically justify its own actions on
470 a regular basis (Lazarus 2009). The law may also delegate the authority to set policy on
471 government's behalf to an independent carbon agency (Helm et al. 2003). Independent
472 agencies which are more insulated from political pressures tend to have stronger
473 incentives to build up and retain reputation over longer time horizons than their
474 political principals (Barro and Gordon 1983). Using legislation and delegation in

475 combination may therefore allow the government to credibly commit to a future
476 climate policy by (i) legally enshrining the adjustment rule and (ii) delegating its
477 implementation to an independent carbon agency. The agency retains the flexibility to
478 react to new developments but it does so within the bounds of the adjustment rule.
479 However, delegation may be opposed by all those who think that climate policies should
480 remain within democratically accountable institutions. In addition, electoral competition
481 could provide an incentive for a political party to avoid delegating responsibility for
482 environmental policy in order to remain relevant for voters.

483

484 Some first examples of adjustment rules for climate policy are emerging in Europe. In
485 the UK, the parliament defined long-term abatement targets in statutory law and
486 delegated monitoring duties to a government independent advisory body. Adjustments
487 to abatement targets follow a formal procedure where the advisory body observes
488 developments in the economy, climate science, and international negotiations, and
489 eventually recommends the parliament to adjust abatement targets. At EU level, the
490 emissions cap in the European Union Emissions Trading Scheme (EU ETS) follows a linear
491 reduction trajectory of -1.74% annually since 2013. Directive 2009/29/EC specifies that
492 the reduction factor shall be reviewed and perhaps adjusted after 2020, leaving thereby
493 open for what reasons, in which direction, and to what extent it may change. Even
494 before 2020, the abatement target may be tightened if, amongst others, “*more*
495 *advanced developing countries*” contribute “*adequately*” to global abatement efforts
496 (Art. 28; Directive 2009/29/EC). Such vaguely formulated conditions under which
497 policies are modified may be necessary to capture the multitude of potential outcomes.
498 However, they may also offer loopholes for opportunistic policy change (Dixit, 1996)
499 which undermines the time-consistency of policies rather than providing flexibility to
500 react to unexpected developments. Hence, there is scope to improve institutional
501 design by using adjustment rules that clearly state the conditions under which policy
502 change is likely.

503

504 These considerations are also relevant for the recent debate on how to reform the EU
505 ETS in face of the stark decline of permit prices witnessed recently. For instance, the
506 automatic stabilizers suggested by Battles et al. (2013), which closely follows the spirit
507 of a ‘Taylor rule’ designed to regulate money supply, is a direct expression of a rule-
508 based approach as discussed above. Further, the proposed price floors and ceilings,
509 which require the regulator to alter the supply of emission permits conditional on their
510 market price (Burtraw et al. 2009) can be regarded as a particular form of an adjustment
511 rule. Finally, approaches that hinge on discretion, such as the Independent Carbon
512 Market Authority (Trotignon and de Perthuis 2013), or a Carbon Market Efficiency Board
513 (Manson 2009) do not follow an explicitly stated rule. Yet, in order to establish a
514 reputation for credibility, their behavior has to be consistent with some clearly
515 identifiable explanatory variables. For central banks, empirical evidence suggests that
516 their actions – even though they can exert discretion over the money supply – is well
517 described by a Taylor rule (Whitesell, 2011). Hence, even an institutional setting relying
518 on discretion might help to approximate the rule-based framework outlined above.¹⁰
519
520

521 **6 Conclusions**

522

523 How can regulators provide dynamically efficient incentives for emissions abatement
524 when benefits of climate change mitigation are uncertain? In a setting in which all
525 relevant parameters are known with certainty, a regulator can achieve the first-best
526 optimal outcome by committing to the ex-ante optimal emission target. However, under
527 uncertainty, new information may be revealed after the regulator’s policy is put in place.
528 Uncertainty makes flexibility very valuable. Full commitment to an ex-ante optimal
529 target – which has been identified by previous literature as a remedy to time-
530 inconsistency – leads to suboptimal results under uncertainty. We demonstrate that

¹⁰ Perhaps the main advantage of such discretionary approaches is that they do not require spelling out all contingencies (Grosjean et al. submitted).

531 under uncertainty, the first-best optimal outcome can still be achieved by means of a
532 transparent rule that allows adjustments of the policy level conditional on new
533 information. Commitment to such an adjustment rule can be established by means of
534 legislating a climate law that specifies the rule and adjustment procedures and
535 delegates implementation tasks to a politically independent agency. Legislation of
536 transparent procedures is particularly important because of the difficulty to impartially
537 evaluate and respond to new information on critical parameters such as climate
538 sensitivity and climate change damage costs.

539

540 While we have presented an argument in favor of adjustment-rule-based policy within a
541 stylized model that focuses on the uncertainty over climate change damage costs, the
542 underlying intuition appears to be relevant to a broader set of applications. In cases in
543 which there is uncertainty with regard to a parameter relevant to decision making that
544 can be observed ex-post, using adjustment rules as a basis of policy can help to mitigate
545 the trade-offs between commitment and flexibility. Such parameters could include not
546 only climate change damage costs but also other important values such as climate
547 sensitivity, sea level rise, economic growth, or even the emissions of other states. Given
548 the many uncertain factors and the need to encourage long-term thinking and
549 investment, adjustment rules could turn out to be an essential ingredient of prudent
550 climate policy.

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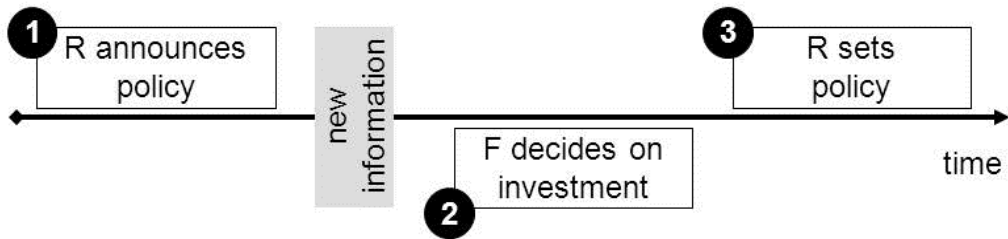
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638 **Appendix: Figures**

639

640



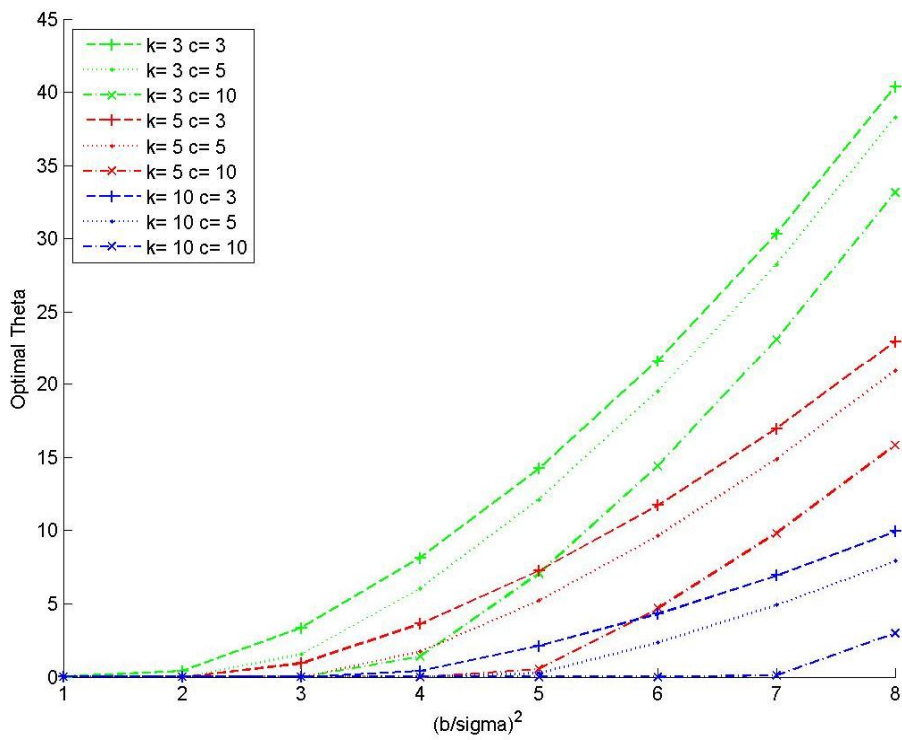
641

Figure 1: Emissions game between regulator (R) and firm (F) under uncertainty

642

643

644



645

Figure 2: Optimal level of commitment for different values of the parameters k and c

646

647